

Quadratic Theory of the Riemann Hypothesis and Connection to Operators and Random Matrix Theories.

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## ABSTRACT

In a bold move, the non trivial zeros of the Riemann Zeta functions are considered as complex zeros of a canonical quadratic equation. The Riemann Hypothesis confirmation and its links to operators and Random Matrix Theories are the direct mathematical implications of this bold view.

**KEYWORDS:** Riemann Zeta function, Riemann Hypothesis, Nontrivial zero, complex zero, spectral analysis, quadratic equation, discriminant, Random Matrix, Quantum chaos, Quasi-crystal, Hermitian operator, Hilbert space Eigenfunction, Eigenvalue, Hilbert-Polya, Connes, Berry and Keating, Casimir, Laplace-Beltrami, Selberg, Number Theory.

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## SHORT PROOF

Let  $s$  be a nontrivial zero of the Riemann Zeta-function. So is  $(1-s)$  by direct application of the Riemann zeta functional equation. ( see E.C. Titchmarsh, "The Theory of the Riemann Zeta-Function", 2<sup>nd</sup> edition, revised by D.R. Heath-Brown, Oxford: Clarendon Press, 1986, page 22, Equation 2.6.4).

...Therefore  $s$  and  $(1-s)$  may be considered as the unique complex zeros of the unique canonical quadratic equation  $Z^2 - S Z + P = 0$ , where  $S = s + (1-s)$  or  $S = 1$ , and  $P = s(1-s)$  and  $P$  non null, and  $Z$  a complex variable, and under the following mathematical constraints:

1-

The related associated discriminant

$$\Delta = S^2 - 4 P$$

must be such that

$$\Delta < 0$$

2-

$$\text{Res}(s) = S/2$$

3-

$$\text{Im}(s)^2 = (-\Delta) / 4$$

These mathematical constraints impose:

a)

$$s(1-s) = [\text{Re}(s)]^2 + [\text{Im}(s)]^2,$$

hence a real and strictly positive number that can be associated with an Eigenvalue  $\lambda$  of a positive, differential, Hermitian, self-adjoint operator  $\partial (1 - \partial)$  defined on some Hilbert spaces, such that

$$\partial (1 - \partial) f = s (1 - s) f = \lambda f,$$

where  $f$  is a Hilbertian Eigenfunction.

See Hilbert-Polya, Aneva, Berry-Keating, Connes, Casimir, and Laplace-Beltrami-Selberg operators .

Therefore the spectral interpretations of the nontrivial Riemann Zeta-zeros are validated.

b)

Real part  $\text{Re}(s)$  is such that

$$\text{Re}(s) = S/2$$

or

$$\text{Re}(s) = 1/2$$

because

$$S = 1.$$

Therefore:

- 1) the Riemann Hypothesis is true,
- 2) its original Hilbert-Polya spectral interpretation is valid, and
- 3) its connection to the Random Matrix Theory goes beyond the special case of the Gaussian Unitary Ensemble (GUE).

#RiemannHypothesis #RiemanHypothesisSolved2014 #GSR.  
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