

# Local lighting and surface models

## COM3404

Richard Everson

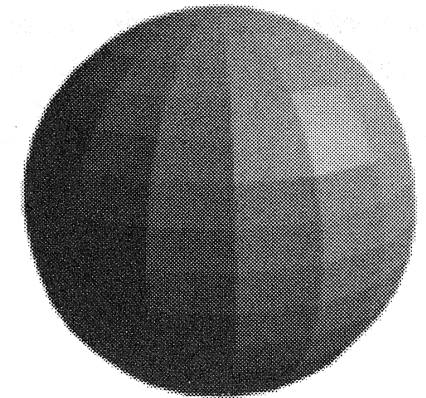
School of Engineering, Computer Science and Mathematics  
University of Exeter

`R.M.Everson@exeter.ac.uk`  
`http://www.secamlocal.ex.ac.uk/studyres/COM304`

# Outline

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- ① Camera and viewing
- ② Rendering polygonal models with shading
- ③ Lights and shading
- ④ Interpolative shading



## References

- Fundamentals of 3D Computer Graphics. Watt. Chapters 4, 5 & 6.
- Computer Graphics: Principles and Practice. Foley et al (1995). Chapters 15 & 16.

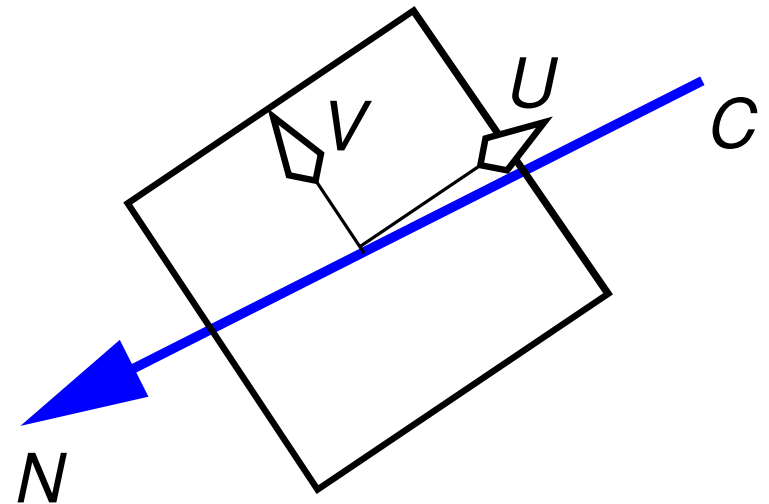
# Camera and viewing

- Scene constructed in world coordinates independently of camera
- Location of the camera determines view of the scene

## Camera parameters

Specified in world coordinates

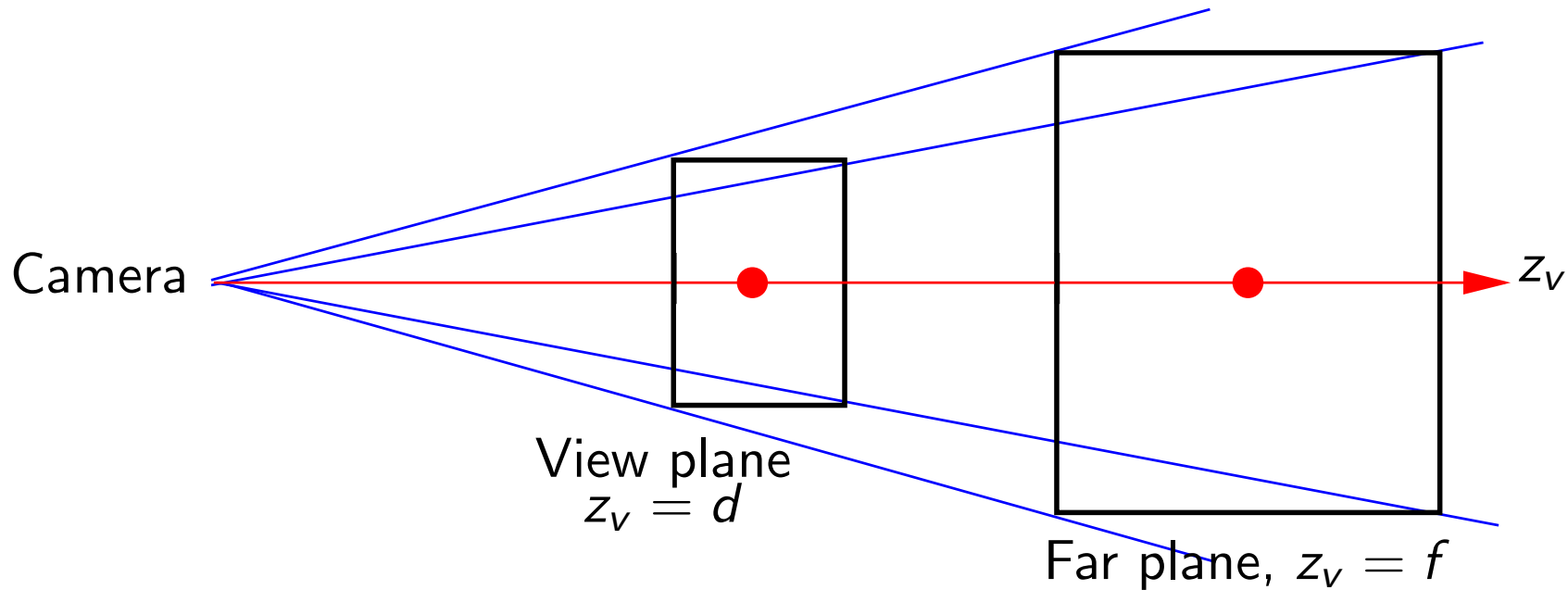
- Location,  $\mathbf{C}$
- Direction:  $\mathbf{N}$  normal to viewing plane along line of sight
- Angle of viewing plane set by orientation of  $\mathbf{U}$  and  $\mathbf{V}$  vectors.
- Field of view: set by viewing frustum
- Depth of field – the area around the focal length that is in focus.



## Animation

Location and other viewing parameters may be animated like other objects in the scene.

# View space to screen space



- Scene clipped to near and far clipping planes
- View plane and near clipping plane usually coincide.
- View plane extends from  $-h \leq x_s, y_s \leq h$
- Transformation to screen (in view plane) accomplished by perspective transformation  $\mathbf{T}_{pers}$

# Viewing transformation

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Transform points from world coordinates to viewing space

$$\begin{bmatrix} x_v \\ y_v \\ z_v \\ 1 \end{bmatrix} = \mathbf{T}_{view} \begin{bmatrix} x_w \\ y_w \\ z_w \\ 1 \end{bmatrix} = \mathbf{RT} \begin{bmatrix} x_w \\ y_w \\ z_w \\ 1 \end{bmatrix}$$

$$\mathbf{R} = \begin{bmatrix} U_x & U_y & U_z & 0 \\ V_x & V_y & V_z & 0 \\ N_x & N_y & N_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \mathbf{T} = \begin{bmatrix} 1 & 0 & 0 & -C_x \\ 0 & 1 & 0 & -C_y \\ 0 & 0 & 1 & -C_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

# View space operations

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## Back face culling

Remove any polygons that face away from the camera. If

- $\mathbf{n}$  is polygon normal
- $\mathbf{v}$  is vector from polygon centre to camera (line of sight vector)

then polygon is visible if

$$\mathbf{v} \cdot \mathbf{n} = |\mathbf{n}| |\mathbf{v}| \cos \theta > 0$$

## Clipping to viewing frustum

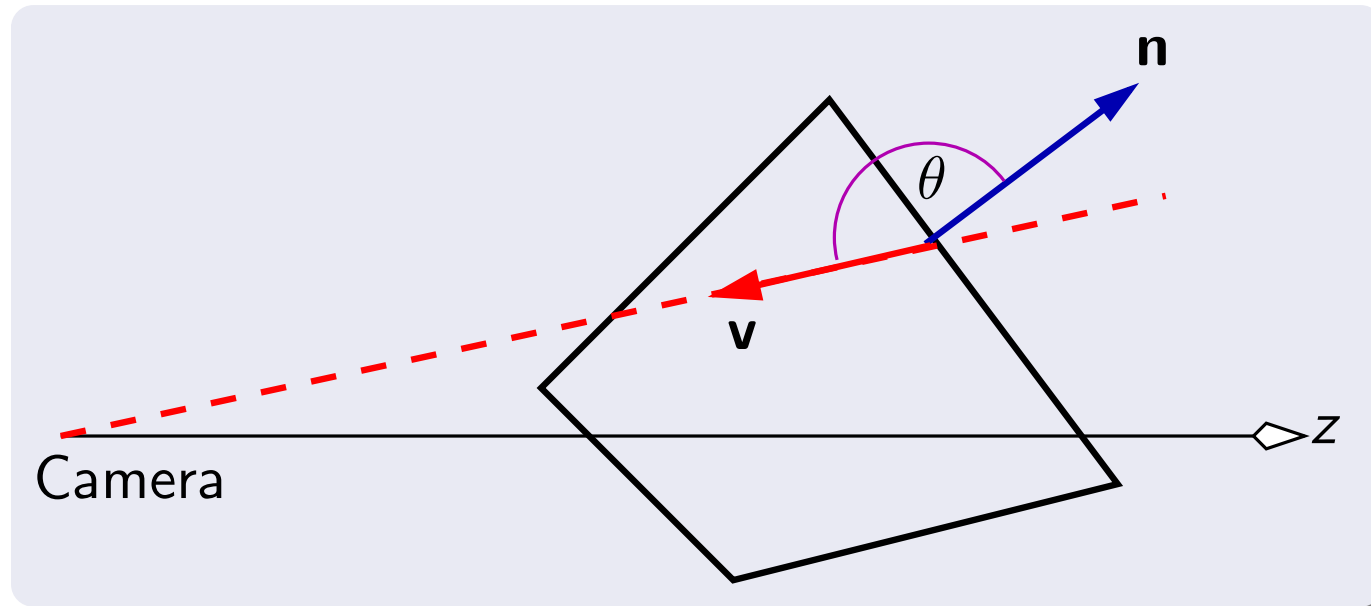
- Clip polygons that are too near  $z_v < d$  or too far  $z_v > f$
- Clip polygons that lie outside the planes

$$x_v = \pm \frac{hz_v}{d} \quad y_v = \pm \frac{hz_v}{d}$$

- Can also be carried out more efficiently in screen space

# Back face culling

Remove any polygons that face away from the camera.



- **n** is polygon normal
- **v** is vector polygon centre to camera (line of sight vector)

Polygon is visible if

$$\mathbf{v} \cdot \mathbf{n} = |\mathbf{n}| |\mathbf{v}| \cos \theta > 0$$

# Perspective transformation

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Transform to *3D screen space* ( $x_s, y_s, z_s$ )

- $x_s, y_s$  coordinates on the screen  $-1 \leq x_s, y_s \leq 1$
- $z_s$  is the apparent depth of the point.

$$\begin{bmatrix} x_s \\ y_s \\ z_s \\ 1 \end{bmatrix} = \mathbf{T}_{pers} \begin{bmatrix} x_v \\ y_v \\ z_v \\ 1 \end{bmatrix} = \begin{bmatrix} d/h & 0 & 0 & 0 \\ 0 & d/h & 0 & 0 \\ 0 & 0 & f/(f-d) & -df/(f-d) \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} x_v \\ y_v \\ z_v \\ 1 \end{bmatrix}$$

Overall transform from world to screen coordinates is

$$\begin{bmatrix} x_s \\ y_s \\ z_s \\ 1 \end{bmatrix} = \mathbf{T}_{pers} \mathbf{T}_{view} \begin{bmatrix} x_w \\ y_w \\ z_w \\ 1 \end{bmatrix}$$

- Render point at  $(x_s, y_s)$
- Use apparent depth to determine what is visible



# Coordinates and transformations

$$\mathbf{x}_s = \mathbf{T}_{pers} \mathbf{T}_{view} \mathbf{x}_w$$

$$\mathbf{x}_s = \mathbf{T}_{pers} \mathbf{x}_v$$

**World coordinates**  $\mathbf{x}_w = (x_w, y_w, z_w)$

Coordinates in which scene is constructed.

**View space**  $\mathbf{x}_v = (x_v, y_v, z_v)$

Coordinates of the scene relative to the camera's point of view

**Viewing transformation**  $\mathbf{T}_{view}$

Transformation describes the camera's view on the scene.

Maps world coordinates to view space.

**3D screen space**  $\mathbf{x}_s = (x_s, y_s, z_s)$

Coordinates of points in the viewing plane, together with apparent depth.

**Perspective transformation**  $\mathbf{T}_{pers}$

Maps view space to 3D screen space

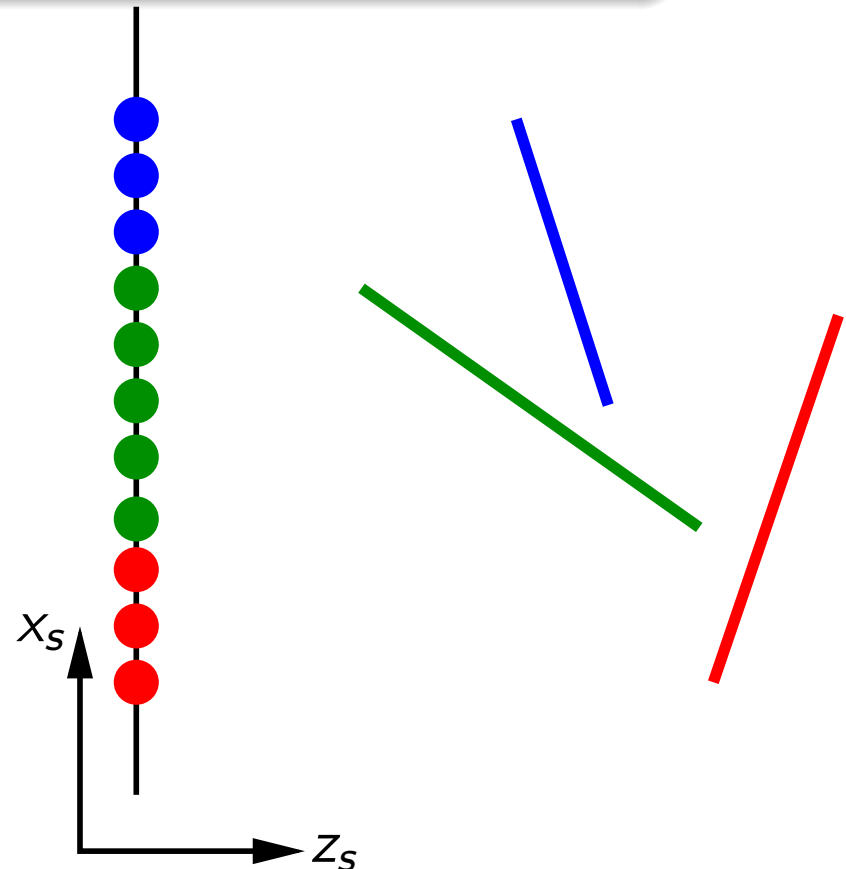
# Rendering polygonal models with shading

Determine rendered colour/shade of each polygon from:

- light falling *directly* on it from a light source;
- surface properties of the polygon.

**Visibility** Many polygons may have the same screen coordinates  $(x_s, y_s)$  but different  $z_s$ : how to determine which is rendered?

**Lighting** How to determine the rendered colour and intensity of a polygon of a particular colour illuminated by a light of a particular colour located in a particular position?



# Z-buffer algorithm

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## Z-buffer

Buffer with an entry for every pixel on the screen.

Contents of  $(x_s, y_s)$  element is the transformed surface that is closest to the screen at  $(x_s, y_s)$

- ① initialise all elements of  $Z_{buf}$  to max-depth
- ② foreach polygon  $P$  in the model
- ③   transform vertices of  $P$  to 3D screen coordinates  $(x_s, y_s, z_s)$
- ④   if  $z_s < Z_{buf}(x_s, y_s)$  for a vertex
- ⑤      $Z_{buf}(x_s, y_s) = z_s$
- ⑥   shade the polygon (in screen coordinates)  
    by interpolating vertex shades
- ⑦   end
- ⑧ end

# Z-buffer

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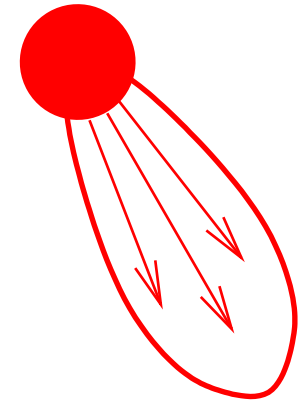
- Z-buffer usually supported in hardware
- Quality of rendering is dependent on resolution of buffer; 20-32 bits is usual. Depth ( $z$ ) values scaled to use full range of Z-buffer.
- Polygons can be processed in any order.
- Independent of model representation (CSG, volumetric, polygonal, etc).
- Scan-line versions exist: less memory, but considerably more complex.
- Cannot cope with transparent or partially transparent polygons, because if the transparent polygon is at the front a list of those behind it must be kept.

# Types of light

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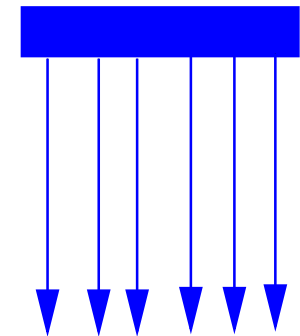
## Spot lights

- Directed
- Intensity decays away from source
- Parameters: location, direction, colour, intensity, decay, drop-off



## Area or rectangular light

- Rectangular beam of parallel rays
- Parameters: location, colour, intensity, direction



## Ambient light

- Simulates the overall light in a space
- Not directed or located
- Parameters: colour, intensity

## Directional light

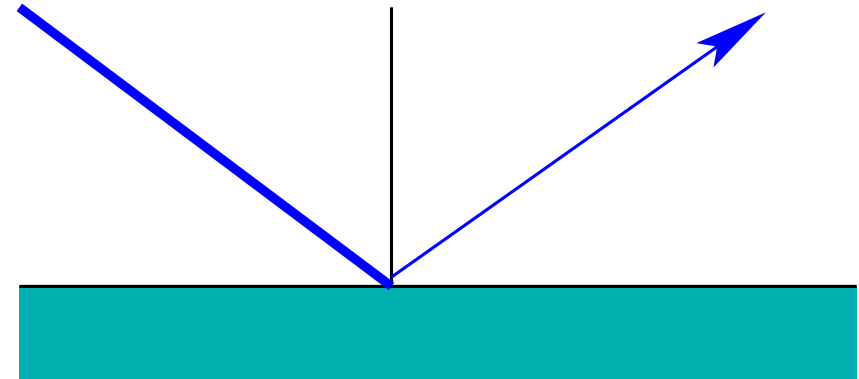
- Located at infinity
- Illuminates scene uniformly from one direction
- Used to simulate sunlight

# Specular reflection

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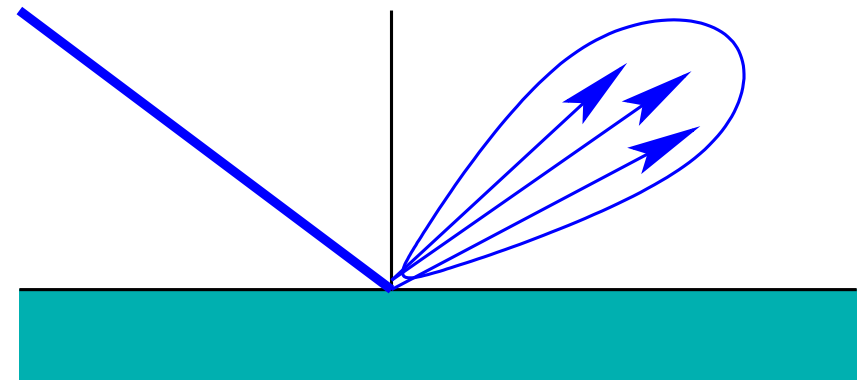
## Perfect specular reflection

- Reflection from a perfect mirror.
- Incident and reflected light make equal and opposite angles with surface normal.



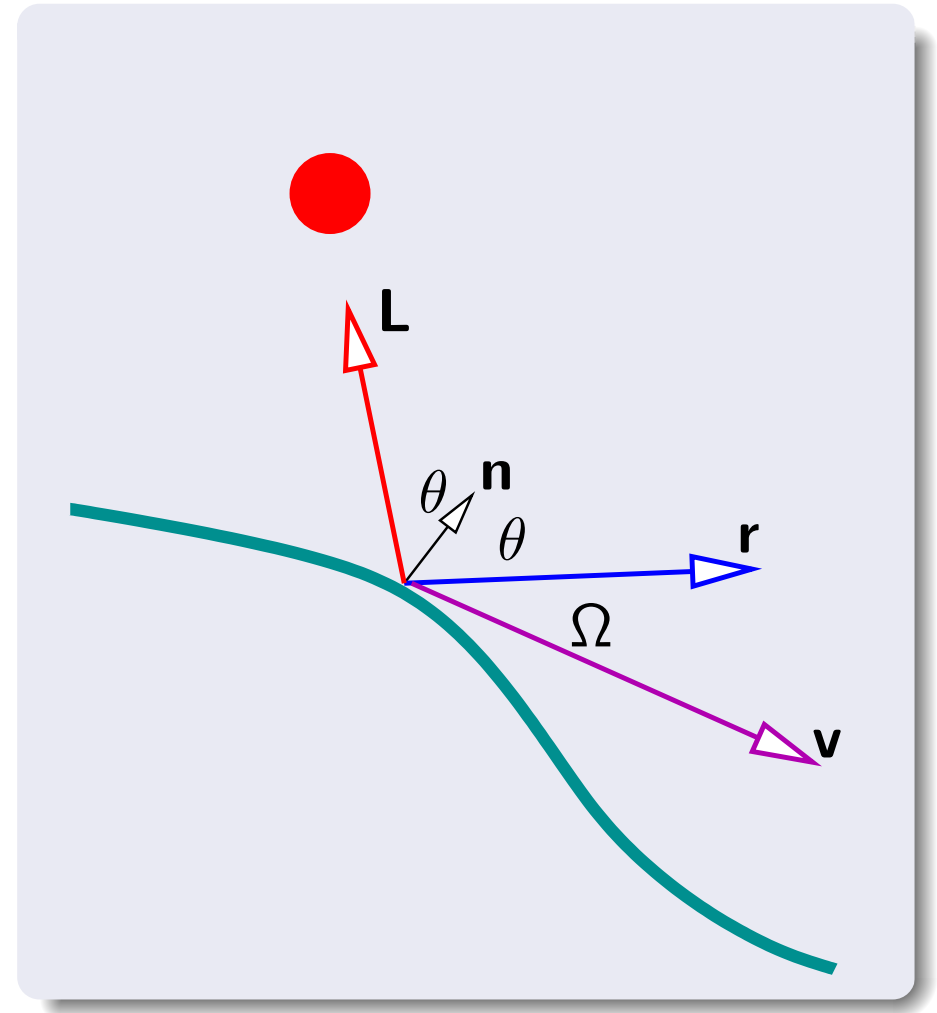
## Imperfect specular reflection

- Some light is scattered away from principal reflected direction.



# Reflection geometry

- $I$  incident intensity
- $I_s$  specular reflected intensity
- $\mathbf{r}$  'mirror' direction
- $\mathbf{v}$  viewing direction
- $\mathbf{L}$  direction to light
- $\mathbf{n}$  surface normal



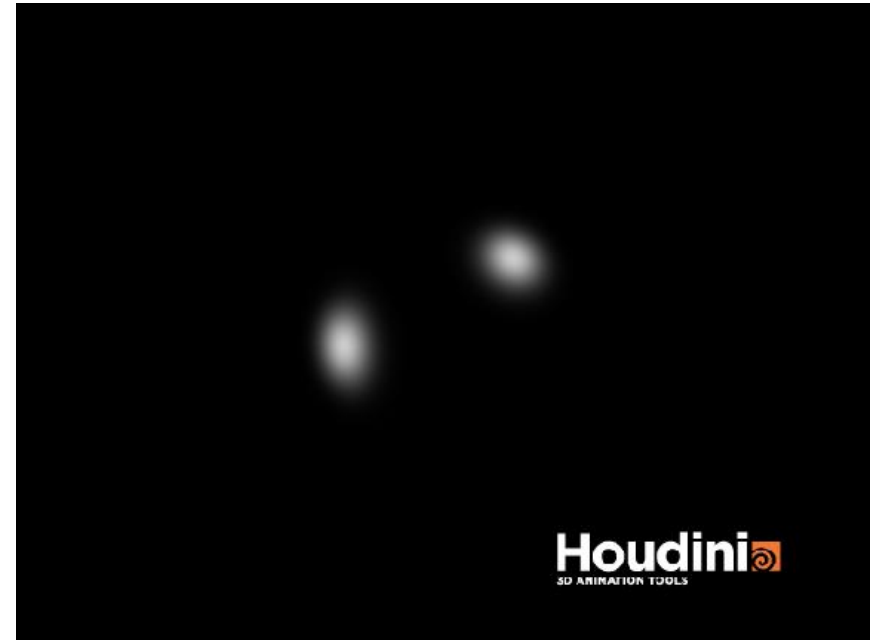
# Specular reflection

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Model specular reflection as

$$I_s = I(\mathbf{r} \cdot \mathbf{v})^n = I(\cos\Omega)^n$$

$n \rightarrow \infty$  for perfect specular reflection



Imperfect specular reflection from two sources

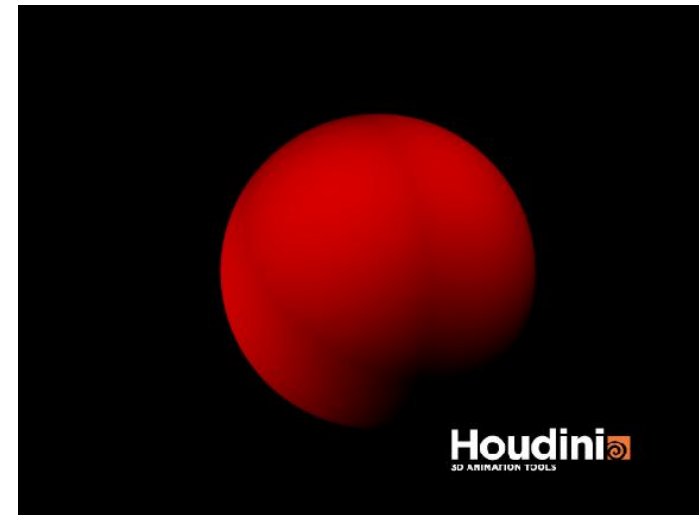
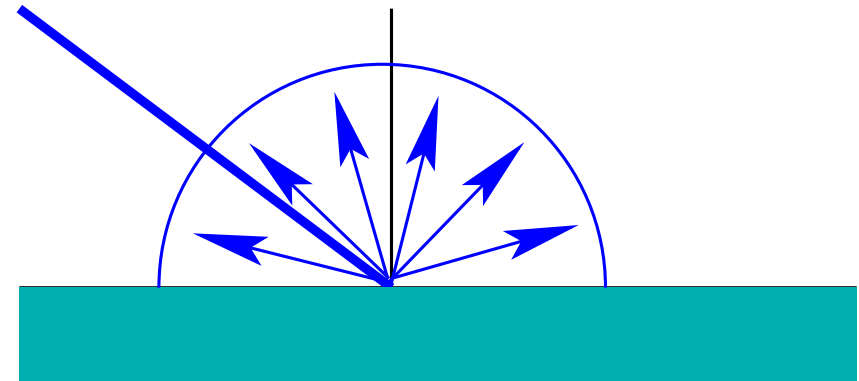


# Diffuse reflection

- Light reflected with equal intensity in all directions
- Modelled as

$$I_d = I \cos \theta = I \mathbf{n} \cdot \mathbf{L}$$

where  $\mathbf{n}$  is the direction of the surface normal.



# Phong reflection model

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Model the combined contributions to light intensity of a surface as

$$\begin{aligned} I_r &= k_a I_a + k_s I_s + k_d I_d \\ &= k_a I_a + I [k_s (\mathbf{r} \cdot \mathbf{v})^n + k_d \mathbf{n} \cdot \mathbf{L}] \end{aligned}$$

where

$$k_s + k_a \leq 1$$

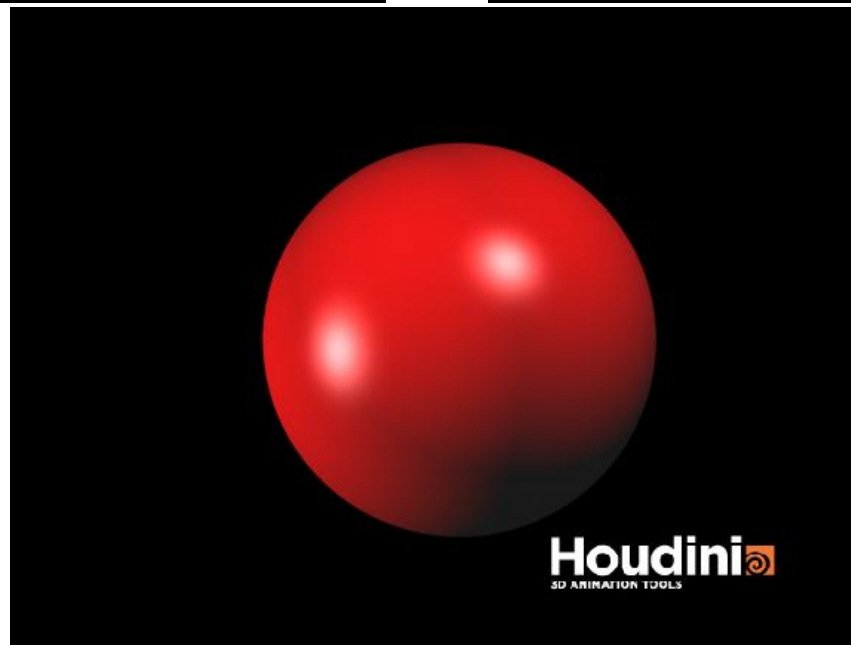
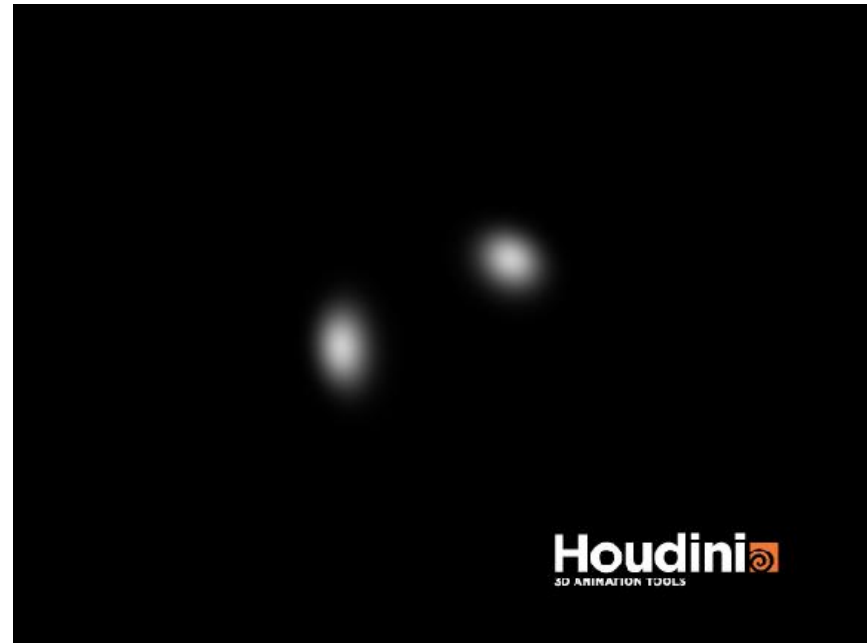
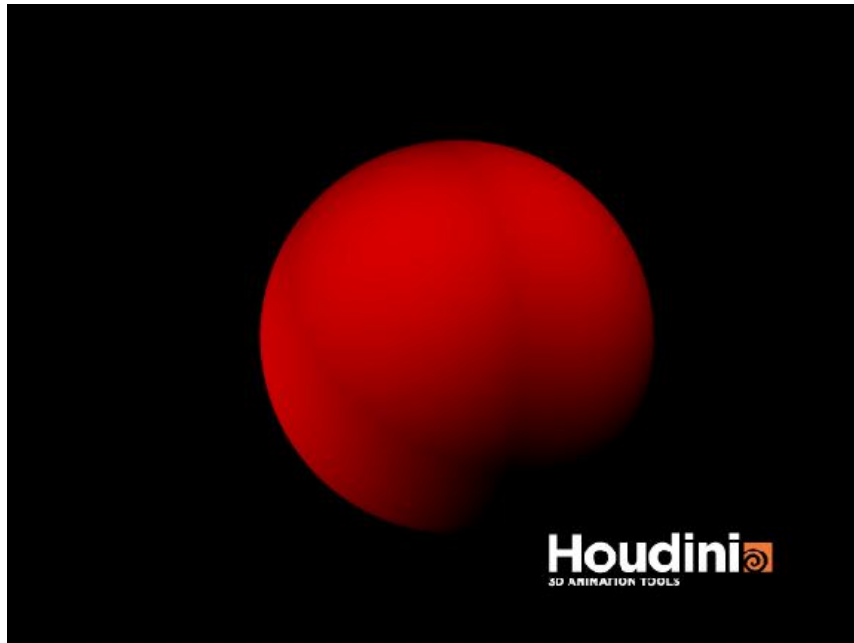
set characteristics of the surface.

- Reflected light from all sources must be summed.
- Each R, G, B component is treated separately.
- Model is a *local* model: light is not reflected from surface to surface.
- Light source itself is taken as a point source at infinity, but the spatial variation of the light can be modelled:

$$I = I_0 (\cos \phi)^m = I_0 (-\mathbf{L} \cdot \mathbf{L}_s)^m$$

where  $\mathbf{L}_s$  is the principal direction of the light source and  $\phi$  is the angle between  $\mathbf{L}$  and  $\mathbf{L}_s$

# Phong reflection model



# Phong reflection



Horizontally  $K_s = 0, 0.2, 0.4, 0.6, 0.8, 1.0$ ; Vertically  $K_d = 0, 0.2, 0.4, 0.6, 0.8, 1.0$ ;  
 $K_a = 0.7, n = 10$

# Interpolative shading

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- 1 Use Z-buffer algorithm to determine screen locations of vertices
- 2 Shade polygons in *screen space* by

**Flat shading** Shade determined by polygon normal and colour at 'centre'

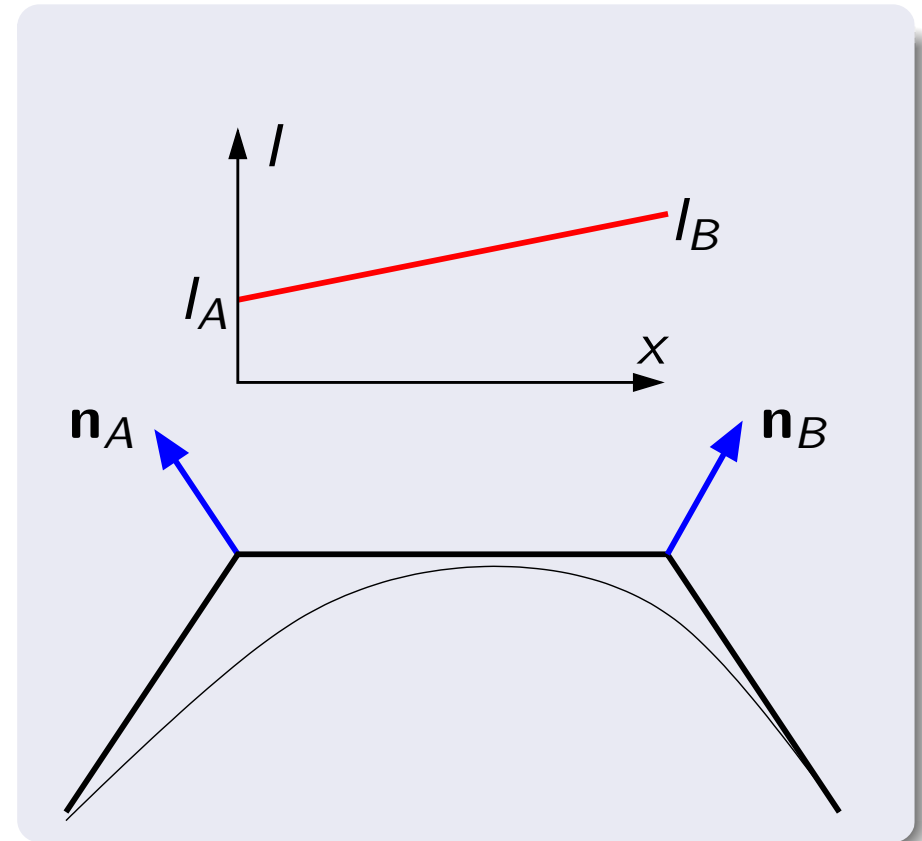
**Gouraud shading** Calculate shades at vertices and interpolate to interior pixels

**Phong shading** Interpolate normal direction to interior pixels and then calculate shade



# Gouraud shading

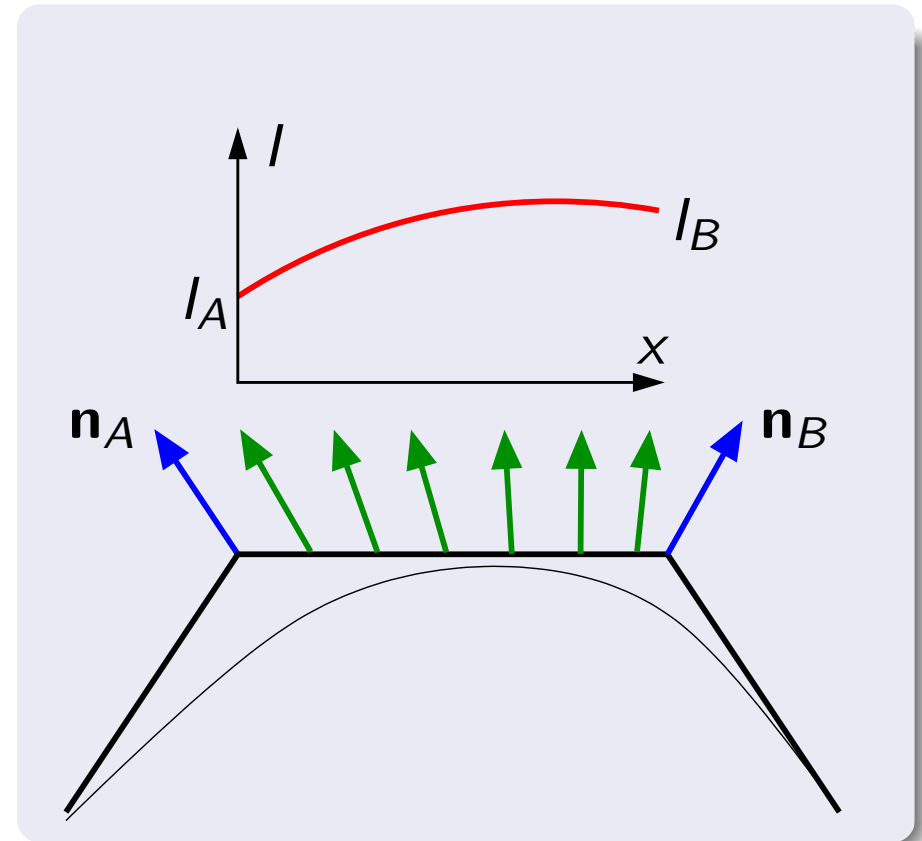
- Calculate vertex normals by (possibly weighted) averaging of adjacent polygons
- (Bi)linearly interpolate intensity between vertices



Efficient scan-line implementation of interpolation.

# Phong shading

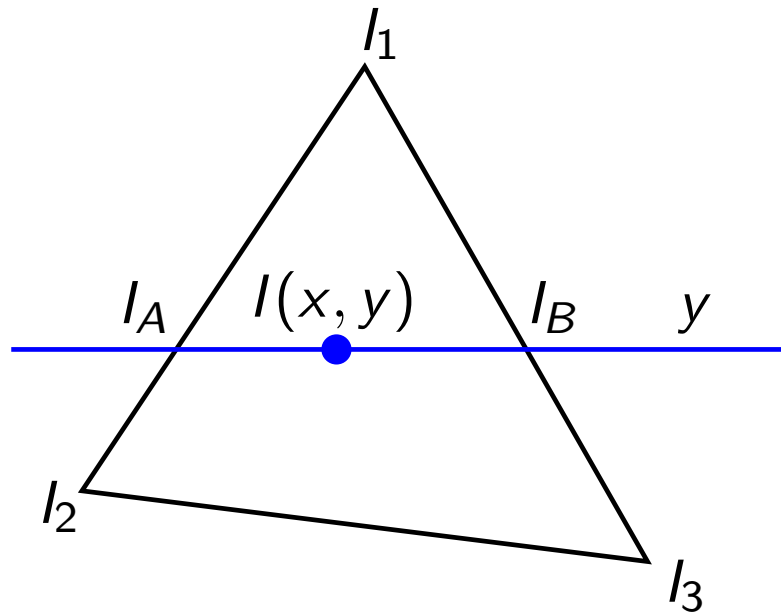
- Calculate vertex normals by (possibly weighted) averaging of adjacent polygons
- (Bi)linearly interpolate *normals* between vertices



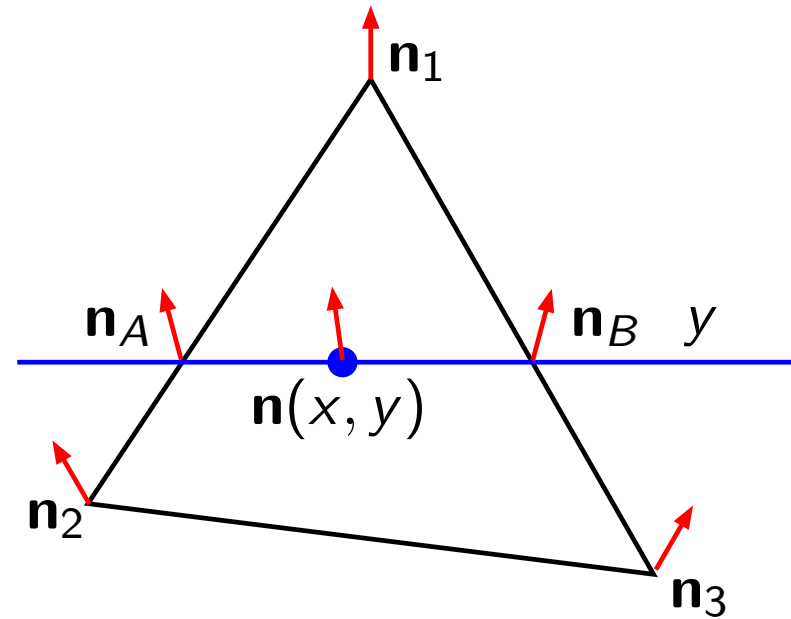
Interpolation of normals restores some 'curvature'

# Scanline interpolation

- Intensities or normals interpolated from vertices along vertices
- Interpolate along scanline from edges



$$\begin{aligned}l_A &= l_{Aprev} + \Delta_{2,1} \\l_B &= l_{Bprev} + \Delta_{3,1} \\l(x_i, y) &= l(x_{i-1}, y) + \Delta_x\end{aligned}$$



$$\begin{aligned}\mathbf{n}_A &= \mathbf{n}_{Aprev} + \Delta_{2,1} \\\mathbf{n}_B &= \mathbf{n}_{Bprev} + \Delta_{3,1} \\\mathbf{n}(x_i, y) &= \mathbf{n}(x_{i-1}, y) + \Delta_x\end{aligned}$$



# Z-buffer algorithm

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- for all  $x, y$ 
  - $Z_{buf}(x, y) := \text{max-depth}$
- for each polygon
  - Convert to edge-based representation in screen coordinates
- for  $y := y_{min}$  to  $y_{max}$ 
  - for each segment in  $EdgeList[y]$ 
    - Interpolate  $X_{left}, X_{right}, Z_{left}, Z_{right}, \mathbf{n}_{left}, \mathbf{n}_{right}$  from segment ends
    - for  $x := X_{left}$  to  $X_{right}$ 
      - interpolate  $z$  and  $\mathbf{n}$
      - if  $z < Z_{buf}(x, y)$ 
        - $Z_{buf}(x, y) := z$
        - $F_{buf}(x, y) := \text{shading}(\mathbf{n})$

# Shading

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**Wireframe** Just draw the edges.

- Very fast, but not beautiful.

**Flat** Use the polygon normal.

- Fast, avoids interpolation.

**Gouraud**

- Basic shading, good for diffuse reflections.
- Poor rendering of highlights and specular reflections.

**Phong** Interpolate normals.

- Highest quality without volumetric rendering
- 4-5 times slower than Gouraud.

**Phong and Gouraud**

- Use Phong for surfaces with specular reflection (large  $k_s$ ).
- Use Gouraud for diffuse surfaces ( $k_s \approx 0$ ).