

Subdivision surfaces COM3404

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Outline

- Subdivision curves
- 2 Subdivision surfaces

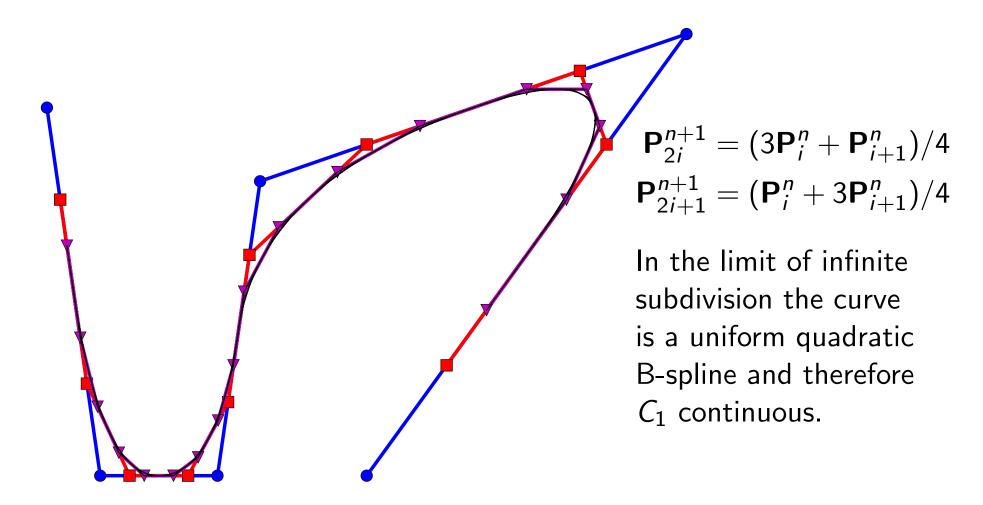


References

- Fundamentals of 3D Computer Graphics. Watt.
- SIGGRAPH 1999 and 2000 course notes: http://mrl.nyu.edu/~dzorin/sig00course/

Subdivision curves: Chaikin

Generate new control vertices at 1/4 and 3/4 along each line segment

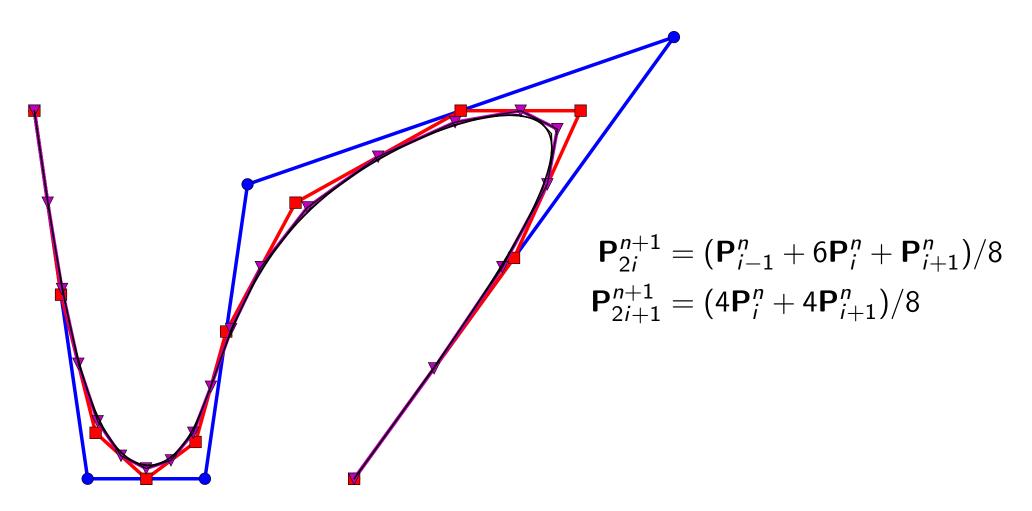


Render (in screen space) by subdivision until line segments are approx
 1 pixel long

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Subdivision curves: C_2 continuity

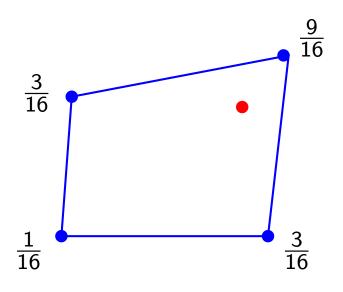
Insert midpoint between vertices and adjust old vertex



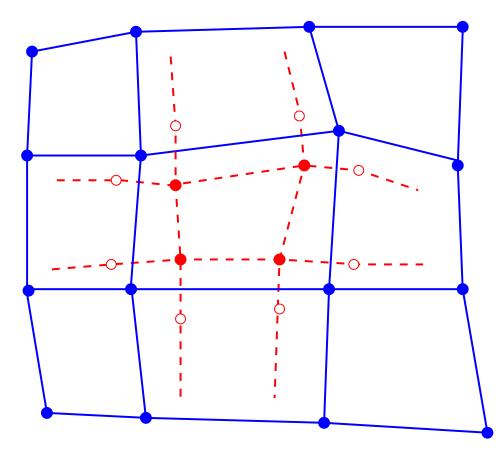
• In the limit of infinite subdivision the curve is a cubic B-spline and therefore C_2 continuous.

Doo-Sabin subdivision

 Generalisation to two dimensions of Chaikin curve subdivision.



• Weights found from $[1/4, 3/4] \times [1/4, 3/4]$



• Render by sub-division until polygons are the size of pixels

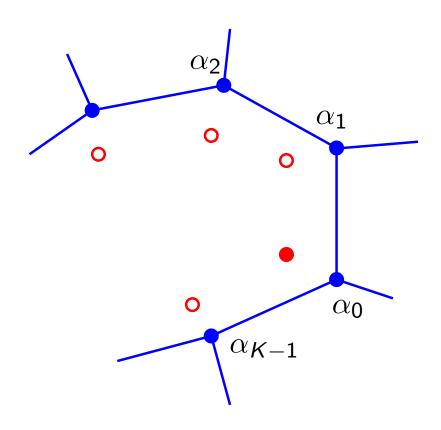
Doo-Sabin extraordinary polygons

- Polygons that are not quadrilaterals are called extraordinary
- In order to preserve continuity of surface in extraordinary polygons Doo-Sabin subdivision requires special weights:

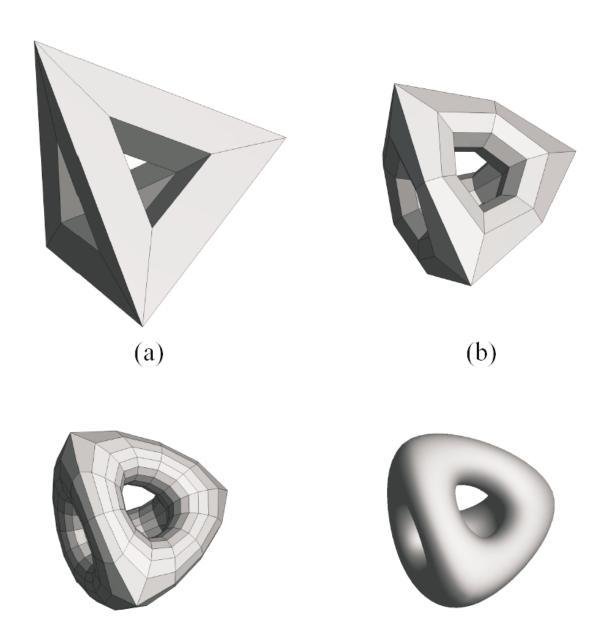
$$\alpha_0 = 1/4 + 5/(4K)$$

 $\alpha_i = (3 + 2\cos(2i\pi/K)/4K)$

K is the *valency*, i.e., the number of vertices

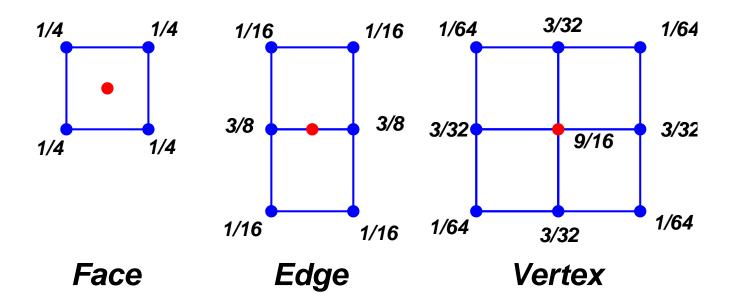


Catmull-Clark subdivision



Catmull-Clark subdivision

- Based on [1, 4, 6, 4, 1]/8 univariate scheme.
- New vertices may be occur in a face, on an edge or at an original vertex



• Obtains C_2 continuity except at extraordinary points where C_1 continuity is achieved with special choices of weight.

Subdivision for animation

Convenient for animation as:

- skeleton can be attached to coarse control points
- always yields a smooth surface (no creases) as skeleton is animated

NURBS Used for:

1995 Toy Story

1998 A Bug's Life

Subdivision surfaces

Piloted in Geri's Game (1997)

Used for:

1999 Toy Story II

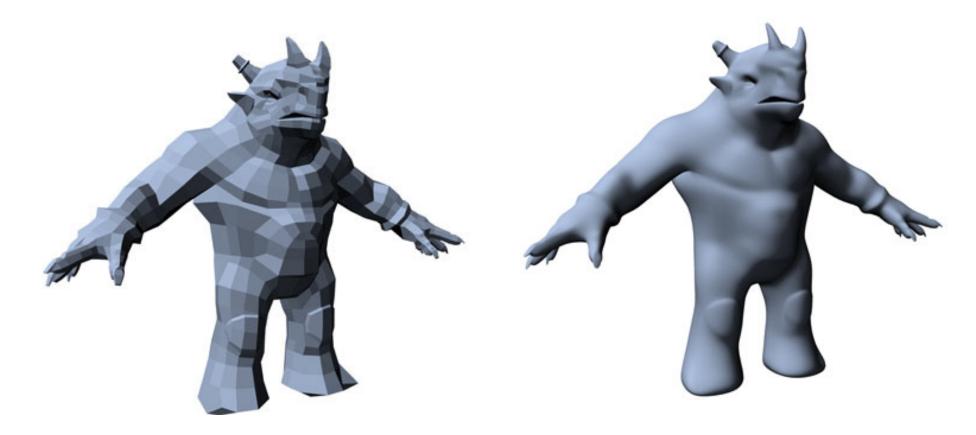
2001 Monsters Inc.

2003 Finding Nemo





Animation and displacement mapping

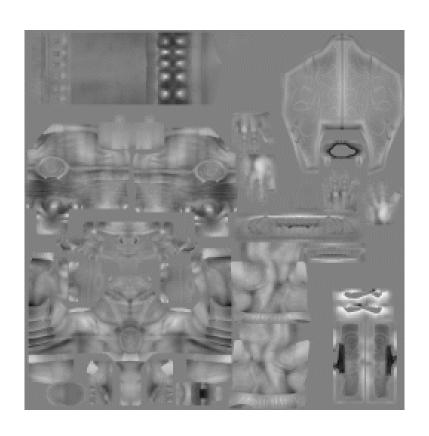


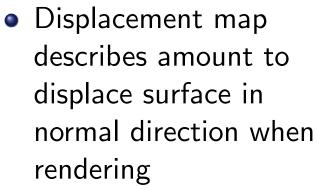
- Rig and animate low resolution model.
- 1,700 polygons

www.fantasylab.com

- Smooth high resolution from sub-division model
- Deforms smoothly when animated.

Animation and displacement mapping







- Smooth sub-division surface plus displacement map
- Equivalent polygon model is 500,000 quadrilaterals

Bézier patches, NURBS and subdivision surfaces

Bézier patches

Difficult to stitch together

NURBS

- Continuity C_1 or C_2 can be guaranteed
- Surfaces require a quadrilateral mesh of control points
- Difficult to join surfaces: extraordinary points
- Very compact representation

Subdivision

- Easy to manipulate
- Handles extraordinary points well
- Not confined to quadrilateral meshes
- Requires lots of memory (but not prohibitive)